# Mining Organizational Structure in Social Network 

## Organizational Structure

- More than simply related or not.
- Reveals the direction of supervision and influence.
- Examples:
- Advisor-advisee relationship
- Terrorist organization hierarchy


## Background

- Community Discovery
- Goal: discover related groups that have denser intra-group communication
- Often reveals interesting properties. Common hobbies, social functions, etc.
- Fail to show power of members and their scope of influence.
- Organizational Structure Discovery
- Good for finding members influential power within the structure.
- Useful in many applications.


## Advisor-Advisee Relationship

Chi Wang, Jiawei Han, Yuntao Jia, Jie Tang, Duo Zhang, Yintao Yu, and Jingyi Guo. Mining advisor-advisee relationships from research publication networks. KDD 'ı.

- Given: publication data with co-author list
- Target: Among those co-authors, find advisor-advisee pairs.
- Used to find experts, or to see students of an expert.


## Example



## Preliminaries

- $a_{i}$ : author $i$
- $a_{y i}$ : advisor of $a_{i}$
- [st ${ }_{i j}$, ed $_{i j}$ ] : time interval that $i$ 's advisor is $j$, i.e., [2003, 2007]
- [ $\mathrm{st}_{i}$, ed ${ }_{i}$ ]: (briefly) time interval that $i$ is advised
- py ${ }_{i}$ : pub_year_vector of $i$ i, i.e., [2003, 2004, 2005]
- $\mathrm{pn}_{i}$ : : :
- py $_{i j}$ : pub_year_vector of co-author $i$ and $j$; link property
- $\mathrm{pn}_{i j}$ : pub_num_vector of co-author $i$ and $j$; link property
- py $_{i}^{1}$ : first component of $\mathrm{py}_{i}$


## Assumptions

1) $\mathrm{ed}_{j}<\mathrm{st}_{i}<\mathrm{ed}_{i}$

- $j$ can only advise $i$ after $j$ graduated.

1) $\mathrm{Py}^{1}{ }_{j}<\mathrm{Py}^{1}{ }_{i j}$

- Advisor $j$ should always have a longer publication history than advisee $i$.


## More Assumptions

- Kulc $c_{i j}$ : Kulczynski ratio. Correlation of two authors' publications
- $I R_{i j}$ : Imbalance ratio between $(j \mid i)$ and $(i \mid j)$
- $j$ is not $i$ 's advisor if
- $I R_{i j}<$ o during the collaboration period. Advisor should have more publications than advisee
- Kulc ${ }_{i j}$ does not increase during the collaboration period
- The collaboration period lasts for only one year
- $p y^{1}{ }_{j}+2>p y^{1}{ }_{i j}$


## Approach Step 1

- Step 1: preprocessing
- Remove unlikely pairs;
- Generate candidate graph, which is a DAG


## Approach Step 2

- TPFG: Time-constrained Probabilistic Factor Graph model
- Let $y_{i}$ be advisor of $\mathrm{a}_{i}$; we need to decide tuple $\left(y_{i}, s t_{i}\right.$, $e d_{i}$ )
- Suppose a local feature function $g\left(y_{i}, s t_{i}, e d_{i}\right)$. Joint probability is defined as

$$
P\left(\left\{y_{i}, s t_{i}, e d_{i}\right\}_{a_{i} \in V^{a}}\right)=\frac{1}{Z} \prod_{a_{i} \in V^{a}} g\left(y_{i}, s t_{i}, e d_{i}\right)
$$

- With assumption 1 as the constraint


## Approach Step 2

- To find most possible relations, maximize the joint probability
- Exhaustive search: $\mathrm{O}\left(\left(\mathrm{CT}^{2}\right)^{\mathrm{n}}\right)$, C candidates/author, with period variable in range $T$.
- Optimize local feature function to find best advising time $\left[s t_{i}, e d_{i}\right]$ for $i$. Only $\left\{y_{i}\right\}$ is left for optimization


## Performance

| data set | RULE | SVM | IndMAX |  | TPFG |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| TEST1 | $69.9 \%$ | $73.4 \%$ | $75.2 \%$ | $78.9 \%$ | $80.2 \%$ | $84.4 \%$ |
| TEST2 | $69.8 \%$ | $74.6 \%$ | $74.6 \%$ | $79.0 \%$ | $81.5 \%$ | $84.3 \%$ |
| TEST3 | $80.6 \%$ | $86.7 \%$ | $83.1 \%$ | $90.9 \%$ | $88.8 \%$ | $91.3 \%$ |

TRAIN1=Colleague(491)+PHD(100)
TEST1=Teacher(257)+MathGP(1909)+Colleague(2166)
TRAIN2=TRAIN3=Teacher(257)+Colleague(2166)
TEST2=PHD(100)+MathGP(1909)+Colleague(4351)
TEST3=AIGP(666)+Colleague(459)

## Issues:

- Need the insight of relationship characteristics.

Difficult to be generalized for other kind of relationships

- How to appropriately interpret the result probabilities: 95\%, 5\%, 51\%
- Real world scenario:
- A is B's advisor in Computer Science;
- B is A's advisor in music;
- Similar amount of publications;
- All possible relations between $s t_{A}, s t_{B}, e d_{A}$, ed ${ }_{B}$, etc.


## Relative Importance in Networks

Scott White and Padhraic Smyth.
Algorithms for estimating relative importance in networks. KDD 'o3.

- Given a relationship network, rank nodes' importance
- Focus: How much "importance" node $t$ inherited from node $r$


## K-Short Node-Disjoint paths

- Why not shortest/closeness/betweenness: longer paths may play important role
- Why node-disjoint: otherwise nodes and edges may appear multiple times in different paths.
- $P(r, t)$ : set of paths from $r$ to $t$.
- $P_{i}$ : the $i^{\text {th }}$ path in $P$
- $\lambda$ :scaling factor

$$
I(t \mid r)=\sum_{i=1}^{|\mathcal{P}(r, t)|} \lambda^{-\left|p_{i}\right|}
$$

## Markov Centrality

- $n$ : number of steps taken
- $f^{n}{ }_{r t}$ : probability the chain first return to $t$ in exactly $n$ steps
- $m_{r t}$ : mean first passage time from $r$ to $t$
- R: given root set

$$
\begin{aligned}
& \text { n root set } \\
& \qquad m_{r t}=\sum_{n=1}^{\infty} n f_{r t}^{(n)} \\
& I(t \mid R)=\frac{1}{\frac{1}{|R|} \sum_{r \in R} m_{r t}}
\end{aligned}
$$

## PageRank with Priors

- $P_{R}=\left\{p_{p}, \ldots, p_{v}\right\}$ : prior probabilities(importances) attached to roots, i.e., $p_{1}=\ldots=p_{v}=1 /|R|$
$-0 \leqslant \beta \leqslant 1$ : probability that we jump back to $R$
- Iterative stationary probability equation:

$$
\pi(v)^{(i+1)}=(1-\beta)\left(\sum_{u=1}^{d_{i_{n}}(v)} p(v \mid u) \pi^{(i)}(u)\right)+\beta p_{v}
$$

- After converge:

$$
I(v \mid R)=\pi(v)
$$

## HITS with Priors

- Similar assumption

$$
\begin{aligned}
H^{(i)} & =\sum_{v=1}^{|V|} \sum_{u=1}^{d_{i n}(v)} h^{(i)}(u) \\
A^{(i)} & =\sum_{v=1}^{|V|} \sum_{u=1}^{d_{o u t}(v)} a^{(i)}(u) \\
a^{(i+1)}(v) & =(1-\beta)\left(\sum_{u=1}^{d_{\text {in }}(v)} \frac{h^{(t)}(u)}{H^{(i)}}\right)+\beta p_{v} \\
h^{(i+1)}(v) & =(1-\beta)\left(\sum_{u=1}^{d_{o u t}(v)} \frac{a^{(t)}(u)}{A^{(i)}}\right)+\beta p_{v}
\end{aligned}
$$

## K-Step Markov

- Random walk starting from R
- Back probability $\beta$
- Fixed-length K
- Compute: Relative probability that the system spend time at any node, after K steps
- A: Markov transition matrix

$$
I(t \mid R)=\left[\mathbf{A} \mathbf{p}_{R}+\mathbf{A}^{2} \mathbf{p}_{R} \ldots \mathbf{A}^{K} \mathbf{p}_{R}\right]_{t}
$$

## 911 European Al Qaeda terrorist network

- Known fact:
- Djamal Beghal has been a leader
- Key roles: Khemais, Maaroufi, Daoudi, and Moussaoui
- 911 leader: Mohammed Atta

| Rank | PRankP | HITSP |  | WKPaths |  | MarkovC |  | KSMarkov |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1: | Khemais | 0.221 | Khemais | 0.173 | Beghal | 0.045 | Atta | 0.063 | Khemais | 0.115 |
| 2: | Beghal | 0.218 | Beghal | 0.166 | Khemais | 0.045 | Al-Shehhi | 0.041 | Beghal | 0.108 |
| $3:$ | Moussaoui | 0.044 | Atta | 0.038 | Moussaoui | 0.045 | al-Shibh | 0.037 | Moussaoui | 0.065 |
| 4: | Maarouii | 0.039 | Moussaoui | 0.029 | Maaroufi | 0.044 | Moussaoui | 0.036 | Maaroufi | 0.059 |
| 5: | Qatada | 0.036 | Maaroufi | 0.026 | Bensakhria | 0.037 | Jarrah | 0.030 | Qatada | 0.052 |
| 6: | Daoudi | 0.035 | Qatada | 0.025 | Daoudi | 0.037 | Hanjour | 0.028 | Daoudi | 0.049 |
| 7: | Courtaillier | 0.032 | Bensakhria | 0.023 | Qatada | 0.036 | Al-Omari | 0.026 | Bensakhria | 0.045 |
| 8: | Bensakhria | 0.031 | Daoudi | 0.023 | Walid | 0.031 | Khemais | 0.025 | Courtaillier | 0.045 |
| $9:$ | Walid | 0.030 | Courtaillier | 0.022 | Courtaillier | 0.031 | Qatada | 0.025 | Walid | 0.040 |
| 10: | Khammoun | 0.025 | Khammoun | 0.021 | Khammoun | 0.029 | Bahaji | 0.024 | Khammoun | 0.034 |

## Coauthership Network

- $R=\{$ Brin, Page, Kleinberg $\}$

| Rank |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| PRankP | HITSP | WKPaths |  | KSMarkov |  |  |  |  |
| 1: | Brin | 0.2014 | Brin | 0.1119 | Kleinberg | 0.0023 | Brin | 0.1045 |
| 2: | Page | 0.1352 | Kleinberg | 0.1107 | Brin | 0.0019 | Motwani | 0.0627 |
| 3: | Kleinberg | 0.1137 | Page | 0.1087 | Motwani | 0.0017 | Ullman | 0.0536 |
| 4: | Motwani | 0.0474 | Motwani | 0.0184 | Raghavan | 0.0016 | Silverstein | 0.0467 |
| 5: | Ullman | 0.0429 | Raghavan | 0.0147 | Page | 0.0014 | Page | 0.0394 |
| 6: | Silverstein | 0.0392 | Ullman | 0.0136 | Silverstein | 0.0014 | Kleinberg | 0.0194 |
| 7: | Raghavan | 0.0111 | Silverstein | 0.0119 | Ullman | 0.0014 | Raghavan | 0.0138 |
| 8: | Lynch | 0.0086 | Williamson | 0.0113 | Williamson | 0.0012 | Zhang | 0.0109 |
| 9: | Kedem | 0.0086 | Papadimitriou | 0.0110 | Vempala | 0.0012 | Guibas | 0.0106 |
| 10: | Williamson | 0.0085 | Lynch | 0.0108 | Indyk | 0.0010 | Robertson | 0.0101 |

## Evolving Networks

Jiangtao Qiu, Zhangxi Lin, Changjie Tang, and Shaojie Qiao. Discovering Organizational Structure in Dynamic Social Network ICDM 'o9

- Algorithm
- Random walk to find the community tree
- Modified PageRank algorithm for m-score computation
- Novalty: min-distance-error evolving tree
- Good for observing power changes
- Insufficient and prelimary results. No comparison to state-of-art.

Thank You!

