



# Similarity Query Processing for High-Dimensional Data

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### Outline

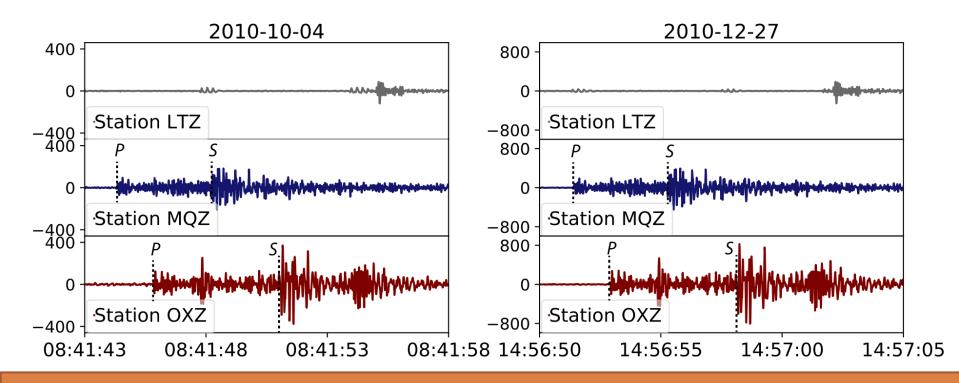
- □ Introduction
- Exact Query Processing
- Approximate Query Processing
- Selectivity Estimation
- □ Open Problems

#### Introduction

- High-dimensional data is abundant
  - Traditional sources:
    - **Time-series** [EZPB19], scientific applications
    - Document, multimedia, strings, feature vectors
  - New data sources:
    - Embedding from deep learning models
- Growing size and complexity
  - Web, social network, IoT
  - NOAA (USA) collects 100TB sensing data / day for weather forecasting
  - A variety of similarity/distance functions concerned

## Example: Scientific Applications

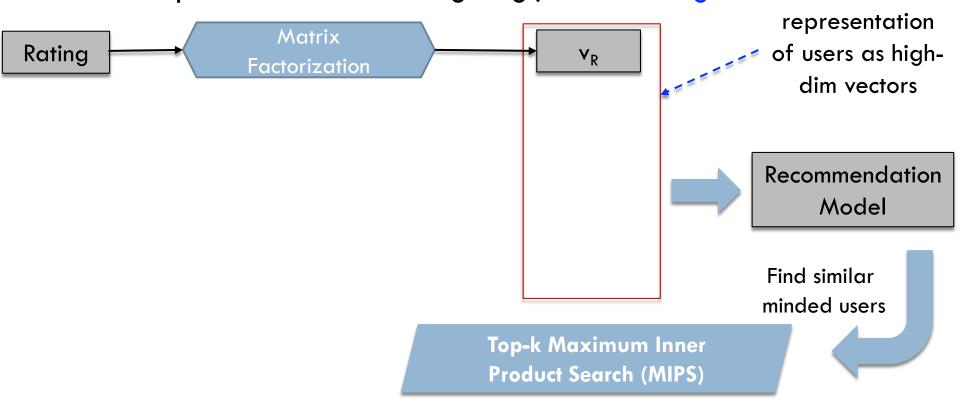
 High-dimensional data in huge volumes in scientific domains [YHEB17, RYBE+18]



Research Question: Whether the magnitude 4.7 earthquake in Arkansa 2011 was caused by wastewater injection

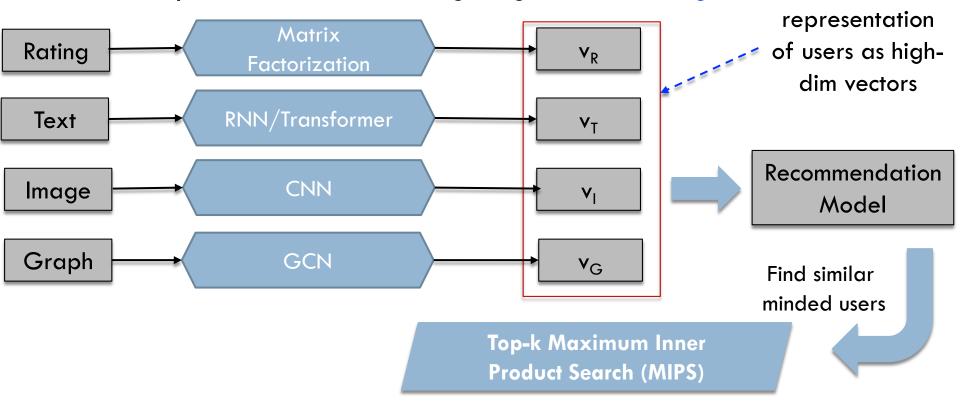
## Example: Embedding Vectors

- DL presents a unified and engineering-friendly way to handle various information sources
  - Representation learning: e.g., embedding



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# Example: Usage in Machine/Deep Learning

- □ Kernel trick
  - $\square \varphi$ : mapping low-dim feature vectors to high-dim vectors

$$\langle \varphi(x), \varphi(x') \rangle = \mathcal{K}(x, x')$$

- □ Feature hashing trick
  - $lue{\varphi}$ : random mapping high-dim feature vectors to low-dim vectors

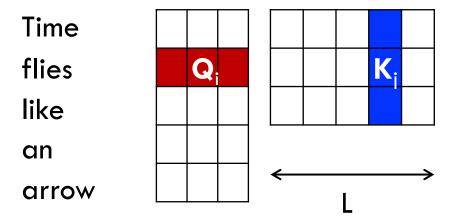
$$\mathbb{E}\left[\left\langle \varphi(x), \varphi\left(x'\right)\right\rangle\right] = \left\langle x, x'\right\rangle$$

Improves efficiency, scalability and sometimes effectiveness

# Example: Usage in Machine/Deep Learning

- □ Reformer [KKL20]
  - Speed up self-attention

Attention(
$$\mathbf{Q}, \mathbf{K}, \mathbf{V}$$
) = softmax  $\left(\frac{\mathbf{Q}\mathbf{K}^{\top}}{\sqrt{d_k}}\right)\mathbf{V}$ 



Find batch top-k  $\mathbf{K}_{i}$ 's for each  $\mathbf{Q}_{i}$ 

Scale to long sequences,  $O(L \log L)$  instead of  $O(L^2)$ 

## Usage in Machine/Deep Learning

- Q-learning with nearest neighbor [SX18]
  - □ Idea:
    - $\blacksquare$  quantization of the state space X into  $\{c_i\}_{i=1}^N$
    - (non-parametric) kernel ridge regression for new (x, a) values

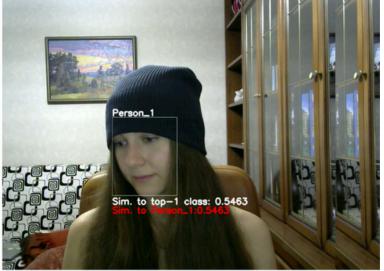
$$\hat{q}(x, a) = \sum_{i=1}^{n} K(x, c_i) q(c_i, a)$$
$$= \sum_{K(c, x) \le h} K(x, c) q(c, a)$$

## Example: Adversarial Machine

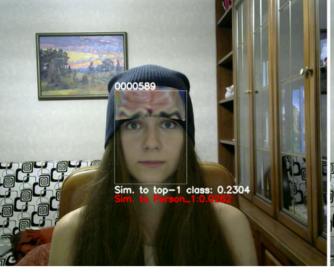
Learning







 $sim \geq 0.54$ 





Adversarial sticker on the forehead

 $sim \leq 0.28$ 

[KP19]

# Example: Adversarial Machine Learning

 Local intrinsic dimensionality (LID) is an important feature to detect adversarial examples [MLWE+18]

$$\widehat{\text{LID}}(x) = -\left(\frac{1}{k} \sum_{i=1}^{k} \log \frac{r_i(x)}{r_k(x)}\right)^{-1}$$

 High-dimensional geometry explains the existence of adversarial examples [GMFS+18] require kNN queries

kNN queries are also useful in

- outlier/novelty detection
- kNN classification
- zero/few-shot learning

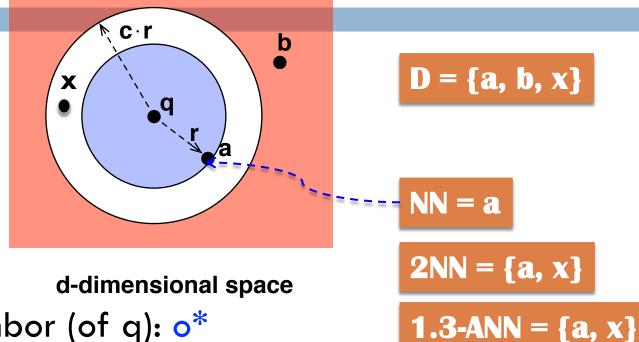
### **Problem Definitions**

- Database object & the query
  - d-dimensional point/vectors ∈ R<sup>d</sup>
- Distance or similarity functions
  - □ dist(u, v) L<sub>p</sub> distar
    - $L_p$  distance (0< $p\le2$ ,  $\infty$ ), Hamming dist, edit dist ...
  - sim(u, v)

cosine similarity/inner product, Jaccard

- Query types
  - k-nearest neighbor queries (kNN)
  - range queries
  - conjunctive queries
  - similarity/distance join queries (top-k, range, closest pair, containment, ...)

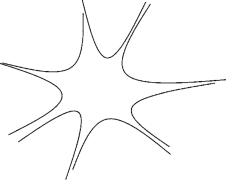
### NN and kNN



- □ Nearest Neighbor (of q): o\*
  - $\square$  dist(o\*, q) = min {dist(o, q), o  $\in$  D}
  - Generalizes to k-NN
- c-Approximate NN: o
  - $\square$  dist(o, q)  $\leq$  c \* dist(o\*, q)

dist() is typically  $L_2$  distance

high-dimensional convex body



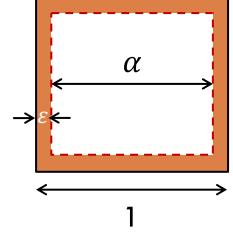
- Non-intuitive high-dimensional Geometry
  - Sampling uniformly within a unit hypercube  $\rightarrow$  samples are within a thin  $\varepsilon$  'shell'

■ Vol(r) = 
$$\alpha^{d} \approx e^{-2\varepsilon d} \rightarrow 0 \ (\alpha < 1)$$

- Angle between two vectors
  - random Radamacher vectors →

$$\Pr\left[\left|\cos\left(\theta_{x,y}\right)\right| > \sqrt{\frac{\log c}{d}}\right] < \frac{1}{c}$$

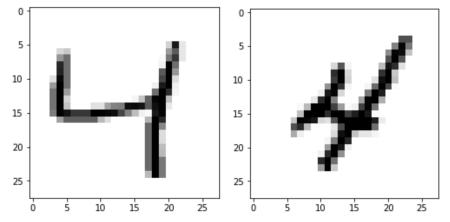
orthogonal w.h.p

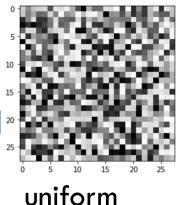


Mohammed J. Zaki, Wagner Meira Jr. Data Mining and Analysis: Fundamental Concepts and Algorithms.

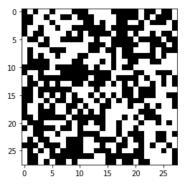
- Curse of Dimensionality / Concentration of Measure
  - Under some assumptions, maxdist(q, D)/mindist(q, D)
     converges to 1
    - Key assumption: independent distribution in each dimension
    - k-NN is still meaningful for real datasets
  - Hard to find algorithms sub-linear in n (# of points) and polynomial in d (# of dimensions)
  - Approximate version (c-ANN) is not much easier

- No idea of the distribution of real data
  - Manifold hypothesis

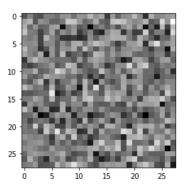




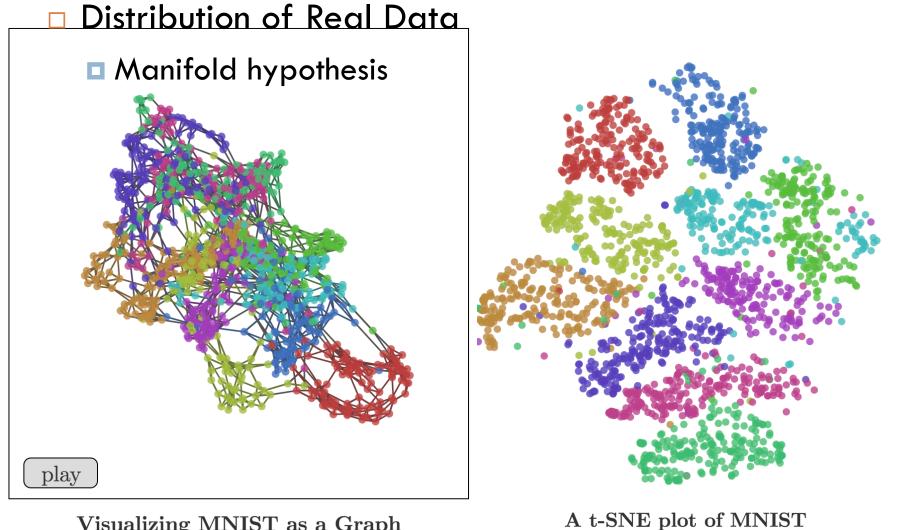
uniform



Radamacher



Gaussian



Visualizing MNIST as a Graph

- Large data size
  - $\blacksquare$  1KB for a single point with 256 dims  $\rightarrow$  1B pts = 1TB
    - ~100 SIFT vectors per image
  - High-dimensionality (e.g., documents → millions of dimensions)
- Variety of distance/similarity functions
  - Less of an issue in the DL era